



10.



11. 
$$\{3,4\}$$
 12.  $\left\{\frac{2+i\sqrt{3}}{2}, \frac{2-i\sqrt{3}}{2}\right\}$ 

**15.** 
$$\left\{-3, \frac{1}{2}, 2\right\}$$
 **16.**  $\{-2\}$ 

17. 
$$\{2\}$$
 18.  $\{-2 + \log_3 11\}$ 

**19.** {625} **20.** 
$$\left\{ \left( -\frac{1}{2}, \frac{1}{2} \right), (2, 8) \right\}$$









$$f(x) = \frac{x^2 - x - 6}{x^2 - x - 6}$$







**29.** 
$$(f \circ g)(x) = 2x^2 - 3x;$$
  
 $(g \circ f)(x) = -2x^2 + x + 2$ 

30. 
$$4x + 2h - 1$$

**31.** 
$$y = -3x + 10$$

**32.** 
$$y = 3x + 3$$

36. 
$$\sec \theta - \cos \theta = \frac{1}{\cos \theta} - \cos \theta = \frac{1 - \cos^2 \theta}{\cos \theta} = \frac{\sin^2 \theta}{\cos \theta} = \frac{\sin \theta}{\cos \theta} \sin \theta = \tan \theta \sin \theta$$

37. 
$$\tan x + \tan y = \frac{\sin x}{\cos x} + \frac{\sin y}{\cos y} = \frac{\sin x \cos y + \sin y \cos x}{\cos x \cos y} = \frac{\sin(x+y)}{\cos x \cos y}$$

38. 
$$\{0, \pi\}$$

**39.** 
$$\left\{0, \frac{\pi}{3}, \frac{5\pi}{3}\right\}$$

# **CHAPTER 9**

## Section 9.1

#### **Check Point Exercises**

**1. a.** 
$$\begin{bmatrix} 1 & 6 & -3 & 7 \\ 4 & 12 & -20 & 8 \\ -3 & -2 & 1 & -9 \end{bmatrix}$$

**b.** 
$$\begin{bmatrix} 1 & 3 & -5 & 2 \\ 1 & 6 & -3 & 7 \\ -3 & -2 & 1 & -9 \end{bmatrix}$$

$$\mathbf{c.} \begin{bmatrix} 4 & 12 & -20 & 8 \\ 1 & 6 & -3 & 7 \\ 0 & 16 & -8 & 12 \end{bmatrix}$$

**2.** 
$$\{(5,2,3)\}$$
 **3.**  $\{(1,-1,2,-3)\}$  **4.**  $\{(5,2,3)\}$ 

#### Exercise Set 9.1

$$\mathbf{1.} \begin{bmatrix} 2 & 1 & 2 & 2 \\ 3 & -5 & -1 & 4 \\ 1 & -2 & -3 & -6 \end{bmatrix}$$

$$\mathbf{2.} \begin{bmatrix} 3 & -2 & 5 & 31 \\ 1 & 3 & -3 & -12 \\ -2 & -5 & 3 & 11 \end{bmatrix}$$

$$\mathbf{3.} \begin{bmatrix} 1 & -1 & 1 & 8 \\ 0 & 1 & -12 & -15 \\ 0 & 0 & 1 & 1 \end{bmatrix}$$

$$\mathbf{4.} \begin{bmatrix} 1 & -2 & 3 & 9 \\ 0 & 1 & 3 & 5 \\ 0 & 0 & 1 & 2 \end{bmatrix}$$

5. 
$$\begin{bmatrix} 5 & -2 & -3 & | & 0 \\ 1 & 1 & 0 & | & 5 \\ 2 & 0 & -3 & | & 4 \end{bmatrix}$$

6. 
$$\begin{bmatrix} 1 & -2 & 1 & 10 \\ 3 & 1 & 0 & 5 \\ 7 & 0 & 2 & 2 \end{bmatrix}$$

7. 
$$\begin{bmatrix} 2 & 5 & -3 & 1 & 2 \\ 0 & 3 & 1 & 0 & 4 \\ 1 & -1 & 5 & 0 & 9 \\ 5 & -5 & -2 & 0 & 1 \end{bmatrix}$$

8. 
$$\begin{bmatrix} 4 & 7 & -8 & 1 & 3 \\ 0 & 5 & 1 & 0 & 5 \\ 1 & -1 & -1 & 0 & 17 \\ 2 & -2 & 11 & 0 & 4 \end{bmatrix}$$

9. 
$$5x + 3z = -11$$
  
 $y - 4z = 12$   
 $7x + 2y = 3$ 

10. 
$$7x + 4z = -13$$
  
 $y - 5z = 11$   
 $2x + 7y = 6$ 

11. 
$$w + x + 4y + z = 3$$
  
 $-w + x - y = 7$   
 $2w + 5z = 11$ 

12y + 4z = 5

12. 
$$4w + x + 5y + z = 6$$
  
 $w - x - z = 8$   
 $3w + 7z = 4$   
 $11y + 5z = 3$ 

$$\begin{array}{c|ccccc}
\mathbf{14.} & \begin{bmatrix} 1 & -4 & 2 & 3 \\ 1 & -4 & 4 & 0 \\ 2 & 0 & 7 & 4 \end{bmatrix}
\end{array}$$

**15.** 
$$\begin{bmatrix} 1 & -3 & 2 & 0 \\ 0 & 10 & -7 & 7 \\ 2 & -2 & 1 & 3 \end{bmatrix}$$

17. 
$$\begin{bmatrix} 1 & -1 & 1 & 1 & 3 \\ 0 & 1 & -2 & -1 & 0 \\ 0 & 2 & 1 & 2 & 5 \\ 0 & 6 & -3 & -1 & -9 \end{bmatrix}$$

$$\mathbf{18.} \begin{bmatrix} 1 & -5 & 2 & -2 & | & 4 \\ 0 & 1 & -3 & -1 & | & 0 \\ 0 & 15 & -4 & 5 & | & -6 \\ 0 & -19 & 12 & -6 & | & 13 \end{bmatrix}$$

**19.** 
$$R_2$$
: -3, -18;  $R_3$ : -12, -15;  $R_2$ :  $-\frac{3}{5}$ ,  $-\frac{18}{5}$ ;  $R_3$ : -12, -1

**19.** 
$$R_2$$
:  $-3$ ,  $-18$ ;  $R_3$ :  $-12$ ,  $-15$ ;  $R_2$ :  $-\frac{3}{5}$ ,  $-\frac{18}{5}$ ;  $R_3$ :  $-12$ ,  $-15$  **20.**  $R_2$ :  $-10$ ,  $-5$ ;  $R_3$ :  $8$ ,  $10$ ;  $R_2$ :  $-2$ ,  $-1$ ;  $R_3$ :  $8$ ,  $10$  **21.**  $\{(1, -1, 2)\}$ 

**22.** 
$$\{(1,-1,1)\}$$
 **23.**  $\{(3,-1,-1)\}$  **24.**  $\{(-3,0,1)\}$  **25.**  $\{(2,-1,1)\}$  **26.**  $\{(4,-3,2)\}$  **27.**  $\{(2,1,1)\}$  **28.**  $\{(0,2,2)\}$  **29.**  $\{(2,-1,1)\}$  **30.**  $\{(1,1,2)\}$  **31.**  $\{(-1,2,-2)\}$  **32.**  $\{(-1,6,3)\}$  **33.**  $\{(1,2,-1)\}$  **34.**  $\{(2,0,-1)\}$  **35.**  $\{(1,2,2)\}$ 

22. 
$$\{(1, -1, 1)\}$$
 23.  $\{(3, -1, -1)\}$  24.  $\{(-3, 0, 1)\}$  25.  $\{(2, -1, 1)\}$  26.  $\{(4, -3, 2)\}$  27.  $\{(2, 1, 1)\}$  28.  $\{(0, 2, 2)\}$  29.  $\{(2, -1, 1)\}$  30.  $\{(1, 1, 2)\}$  31.  $\{(-1, 2, -2)\}$  32.  $\{(-1, 6, 3)\}$  33.  $\{(1, 2, -1)\}$  34.  $\{(2, 0, -1)\}$  35.  $\{(1, 2, 3, -2)\}$  36.  $\{(2, 1, -1, 3)\}$  37.  $\{(0, -3, 0, -3)\}$  38.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0, -2)\}$  39.  $\{(1, 3, 0,$ 

**42.**  $f(x) = -x^3 + 4x^2 - 2$  **43.**  $\{(e^{-1}, e, e^{-3}, e^{-2})\}$  **44.**  $\{(e, e^{-1}, e^2, e^{-3})\}$  **45.** a.  $a = -32, v_0 = 56, s_0 = 0$  b. 0; The ball hits the ground 3.5 seconds after it is thrown. **c.** 1.75 sec; 49 ft **46. a.** a = -32;  $v_0 = 128$ ;  $s_0 = 6$  **b.** s(7) = 118; The ball's height is 118 feet after 7 seconds.

47. 
$$40x + 200y + 400z = 660$$
; 4 oz of Food A;  $\frac{1}{2}$  oz of Food B; 1 oz of Food C  
 $5x + 2y + 4z = 25$   
 $30x + 10y + 300z = 425$ 

48. 2x + 3y + 2z = 100; 15 children's models; 10 office models; 20 deluxe models 2x + y + 3z = 100x + y + 2z = 65

49. Asians: 122; Africans: 28; Europeans: 24; Americans: 9 50. rooms: 132; bathrooms: 35; fireplaces: 28; elevators: 3

**58.**  $\{(1, -1, 2, -2, 0)\}$  **59.** makes sense **60.** makes sense 61. makes sense 62. makes sense

**63.** false **64.** false **65.** false **66.** false **67.** 60 units: \$7700

**68.** For z = 0, (12z + 1, 10z - 1, z) is (1, -1, 0); 3(1) - 4(-1) + 4(0) = 7 is true; 1 - (-1) - 2(0) = 2 is true; 2(1) - 3(-1) + 6(0) = 5 is true.

**69.** For z = 1, (12z + 1, 10z - 1, z) is (13, 9, 1); 3(13) - 4(9) + 4(1) = 7 is true; 13 - 9 - 2(1) = 2 is true; 2(13) - 3(9) + 6(1) = 5 is true.

70. a. Answers may vary. b. This system has more than one solution.

### Section 9.2

#### **Check Point Exercises**

1. 
$$\emptyset$$
 2.  $\{(11t + 13, 5t + 4, t)\}$  3.  $\{(t + 50, -2t + 10, t)\}$  4. a.  $w + z = 15$  b.  $\{(-t + 15, t + 15, -t + 30, t)\}$  c.  $w = 5; x = 25; y = 20$   $x + y = 45$   $y + z = 30$ 

#### **Exercise Set 9.2**

**1.** 
$$\varnothing$$
 **2.**  $\varnothing$  **3.**  $\left\{\left(-2t+2,2t+\frac{1}{2},t\right)\right\}$  **4.**  $\left\{(-2+t,-2+t,t)\right\}$  **5.**  $\left\{(-3,4,-2)\right\}$  **6.**  $\left\{(2,-3,7)\right\}$  **7.**  $\left\{(5-2t,-2+t,t)\right\}$ 

8. 
$$\{(-5+7t,1+3t,t)\}$$
 9.  $\{(-1,2,1,1)\}$  10.  $\emptyset$  11.  $\{(1,3,2,1)\}$  12.  $\{\left(\frac{1}{3}t,\frac{2}{3}t,-\frac{1}{3}t,t\right)\}$  13.  $\{(1,-2,1,1)\}$  14.  $\{(1,-2,3,-4)\}$ 

**15.** 
$$\left\{ \left(1 + \frac{1}{3}t, \frac{1}{3}t, t\right) \right\}$$
 **16.**  $\left\{ \left(2, \frac{1}{2}t - \frac{1}{2}, t\right) \right\}$  **17.**  $\left\{ (-13t + 5, 5t, t) \right\}$  **18.**  $\left\{ (-2t + 3, -2t + 1, t) \right\}$  **19.**  $\left\{ \left(2t - \frac{5}{4}, \frac{13}{4}, t\right) \right\}$ 

**20.** 
$$\{(98, 2t - 43, t)\}$$
 **21.**  $\{(1, -t - 1, 2, t)\}$  **22.**  $\{(t + 3, 5t + 5, 3t + 4, t)\}$  **23.**  $\{\left(-\frac{2}{11}t + \frac{81}{11}, \frac{1}{22}t + \frac{10}{11}, \frac{4}{11}t - \frac{8}{11}, t\right)\}$ 

**24.** 
$$\left\{ \left( \frac{1}{3}t - \frac{2}{3}s, \frac{1}{3}t + \frac{1}{3}s, t, s \right) \right\}$$

**25.** a. 
$$4w - 2x + 2y - 3z = 0$$
;  $7w - x - y - 3z = 0$ ;  $w + x + y - z = 0$  b.  $\{(0.5t, 0, 0.5t, t)\}$ 

**26. a.** 
$$2w + 17x - 23y + 40z = 0$$
;  $2w + 5x + y + 3z = 0$ ;  $x - 2y + 3z = 0$  **b.**  $\{(-5.5t, 2t, t, 0)\}$ 

**27. a.** 
$$w + 2x + 5y + 5z = -3$$
;  $w + x + 3y + 4z = -1$ ;  $w - x - y + 2z = 3$  **b.**  $\{(1 - 3s - t, -2 - s - 2t, t, s)\}$ 

**28.** a. 
$$w + y + z = 0$$
;  $w - x + 2y + 3z = 0$ ;  $3w - 2x + 5y + 7z = 0$  b.  $\{(-s - t, 2s + t, t, s)\}$ 

**29.** 
$$z + 12 = x + 6$$
 **30.**  $y + 6 = z + 8$  **31.**  $\{(t + 6, t + 2, t)\}$  **32.**  $x = 10, y = 6$ 

**33. a.** 
$$w + z = 380$$
 **b.**  $\{(380 - t, 220 + t, 50 + t, t)\}$  **c.**  $w = 330, x = 270, y = 100$   $x - y = 170$ 

$$x - y = 170$$
$$y - z = 50$$

34. a. There is no combination of the foods that can satisfy the given requirements.

b. There are many combinations of the foods that satisfy the new requirements.

35. a. The system has no solution, so there is no way to satisfy these dietary requirements with no Food 1 available.

b. 4 oz of Food 1,0 oz of Food 2,10 oz of Food 3;2 oz of Food 1,5 oz of Food 2,9 oz of Food 3 (other answers are possible).

36. 7 of product A, 2 of product B, 2 of product C; 7 of product A, 1 of product B, 4 of product C (other answers are possible).

**40. a.** 
$$x_1 - x_6 = 100$$
 **b.**  $\{(t + 100, t - s + 600, -s + 900, t + 300, s - 200, t, s)\}$   $x_2 - x_6 + x_7 = 600$ 

$$x_2 - x_6 + x_7 = 600$$

$$x_3 + x_7 = 900$$

$$x_1 - x_4 = -200$$

$$x_2 - x_4 + x_5 = 100$$

 $x_3 + x_5 = 700$ 

41. does not make sense 42. makes sense 43. does not make sense 44. makes sense 45. a = 1 or a = 3 47. -1 48. -12 49. 8

#### Section 9.3

### **Check Point Exercises**

Check Point Exercises

1. a. 
$$3 \times 2$$
 b.  $a_{12} = -2$ ;  $a_{31} = 1$ 

2. a.  $\begin{bmatrix} 2 & 0 \\ 9 & -10 \end{bmatrix}$  b.  $\begin{bmatrix} 9 & -4 \\ -9 & 7 \\ 5 & -2 \end{bmatrix}$ 

3. a.  $\begin{bmatrix} 6 & 12 \\ -48 & -30 \end{bmatrix}$  b.  $\begin{bmatrix} -14 & -1 \\ 25 & 10 \end{bmatrix}$ 

4.  $\begin{bmatrix} -4 & 3 \\ -3 & \frac{13}{3} \end{bmatrix}$ 

5. 
$$\begin{bmatrix} 7 & 6 \\ 13 & 12 \end{bmatrix}$$
 6.  $[30]$ ;  $\begin{bmatrix} 2 & 0 & 4 \\ 6 & 0 & 12 \\ 14 & 0 & 28 \end{bmatrix}$  7. a.  $\begin{bmatrix} 2 & 18 & 11 & 9 \\ 0 & 10 & 8 & 2 \end{bmatrix}$  b. The product is undefined.